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Outline

- Fundamental Matlab usage
- Image Filtering by Using Matlab
- Fourier Transform by Using Matlab
- Reconstructing an Image from Projection Data by using Matlab

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Image Filtering by Using Matlab

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Data types and conversions

- Data type
 - int8, uint8, int16, uint16, double
- Data conversion
 - ind2gray, gray2ind, rgb2gray, gray2rgb, rgb2ind, ind2rgb.
 - How to use? Type help XXX!

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Example: ind2gray

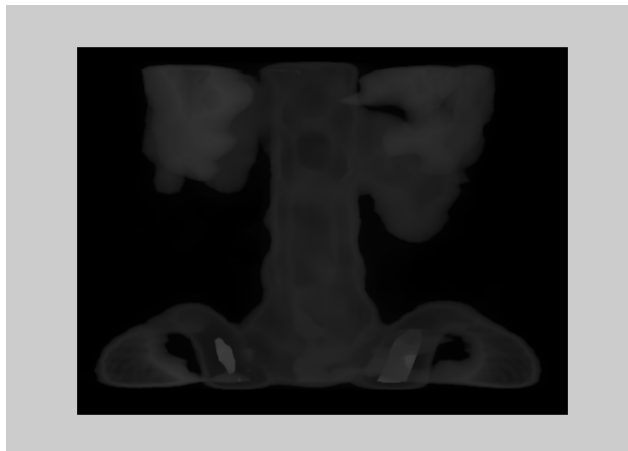
- Usage: Convert indexed image (0-128) to intensity image (0-1)
- Code example
 - load trees;
 - I = ind2gray(X,map);
 - Figure; imshow(X,map);
 - Figure; imshow(I);



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Image import and show

- `>> w=imread('spine.tif');`
- `>> imshow(w);` %w is a uint8 format



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- >> imdistline
- >> impixelinfo



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- imfinfo('spine.tif')

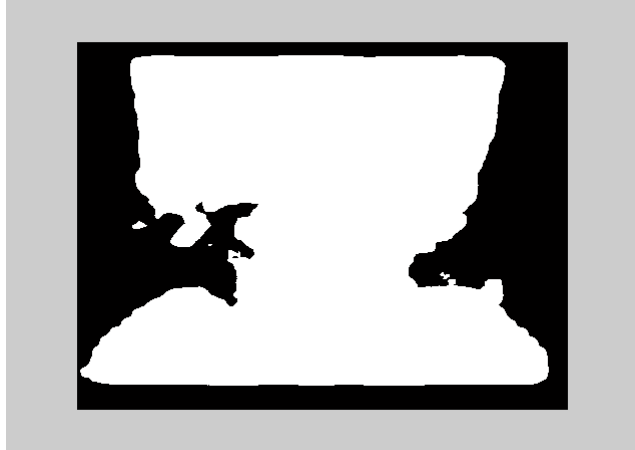
```
Command Window
>> imfinfo('spine.tif')

ans =

    Filename: 'C:\MATLAB7\toolbox\images\indenos\spine.tif'
    FileModDate: '04-Dec-2000 13:57:52'
    FileSize: 69292
    Format: 'tif'
    FormatVersion: []
    Width: 490
    Height: 367
    BitDepth: 8
    ColorType: 'indexed'
    FormatSignature: [73 73 42 0]
    ByteOrder: 'little-endian'
    NewSubfileType: 0
    BitsPerSample: 8
    Compression: 'PackBits'
    PhotometricInterpretation: 'RGB Palette'
    StripOffsets: [23x1 double]
    SamplesPerPixel: 1
    RowsPerStrip: 16
    StripByteCounts: [23x1 double]
```

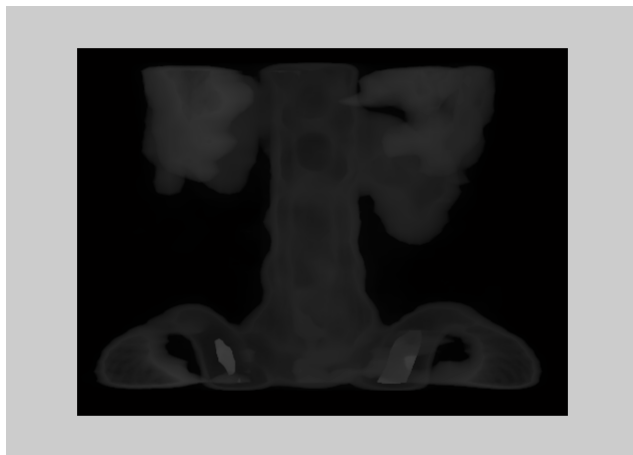
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- `>> w1 = double(w);`
- `>> figure;`
- `>> imshow(w1)`



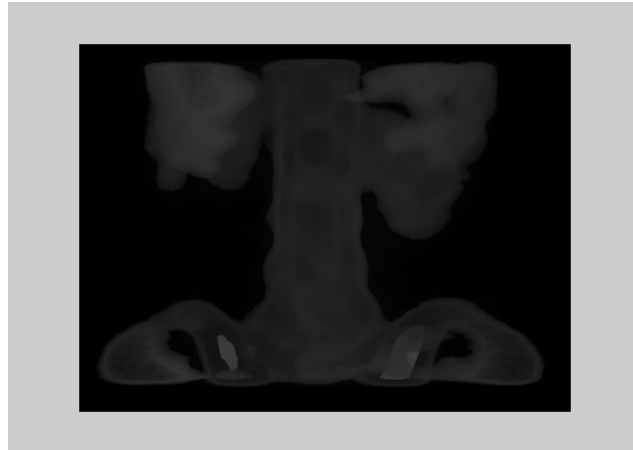
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- Correct the image scale (0 ~1):
 - `>> figure;`
 - `>> imshow(w1/256)`



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- Or use “im2double”:
 - >> w2 = im2double(w);
 - >> figure;
 - >> imshow(w2)



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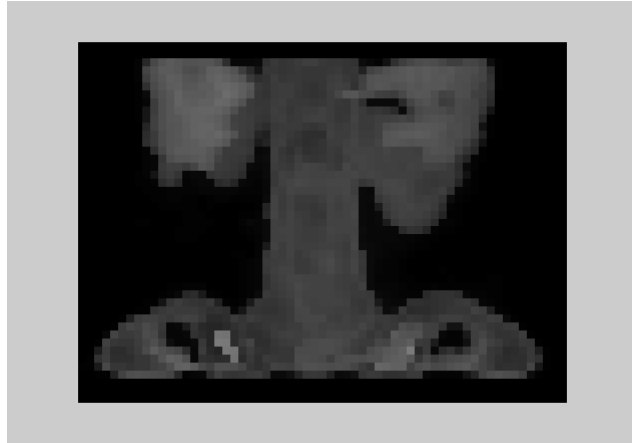
- The simplest way to Increase image contrast:
 - >> w = w*2;
 - >> imshow(w)



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- Change the image resolution:

```
- >> w3 = imresize(imresize(w,1/8),8);  
- >> imshow(w3)
```



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```
- >> w3 = imresize(imresize(w,1/32),32);  
- >> imshow(w3)
```

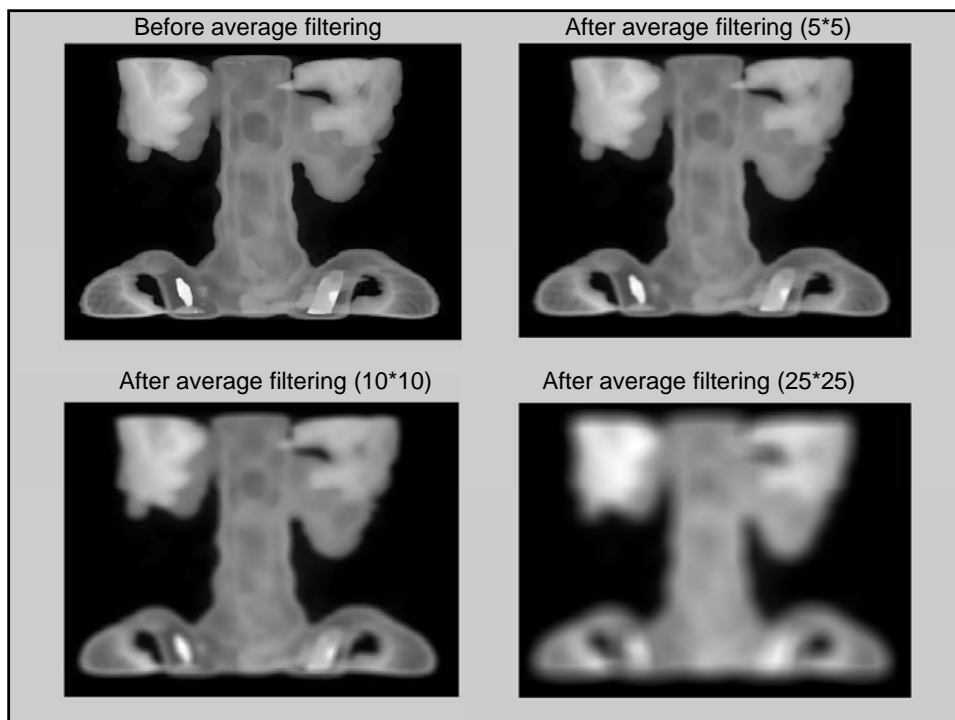


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Image filtering

- Average filtering
 - >> w1 = double(w);
 - >> figure;
 - >> imshow(w1/max(max(w1)));
 - >> f1= fspecial('average',10); % 2-D filter;
 - >> w5 = filter2(f1,w);
 - >> figure;
 - >> imshow(w5/max(max(w5)));

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- A 5*5 averaging filter:
 - `f2= fspecial('average',5);`

```
>> f2
```

```
f2 =
```

```
0.0400    0.0400    0.0400    0.0400    0.0400
0.0400    0.0400    0.0400    0.0400    0.0400
0.0100    0.0100    0.0100    0.0100    0.0100
0.0400    0.0400    0.0400    0.0400    0.0400
0.0400    0.0400    0.0400    0.0400    0.0400
```

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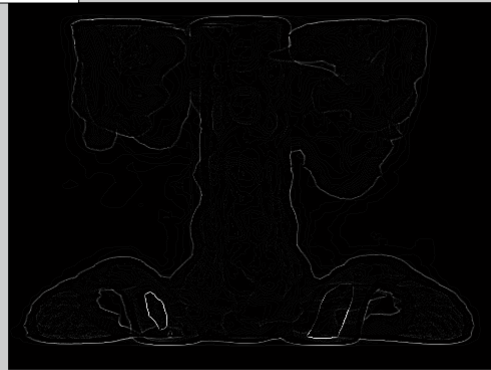
- Average filter is a high-pass filter
- A example of high-pass filter:
 - Laplacian filter
 - Log filter

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```
>> f= fspecial('laplacian')
```

```
f =
```

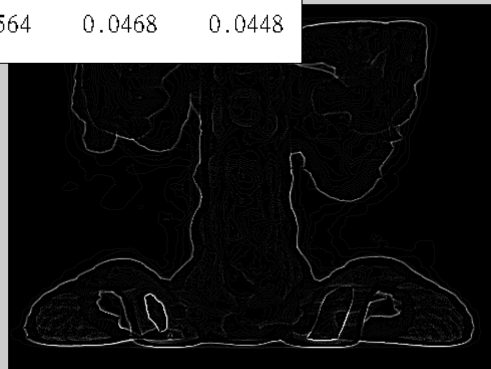
```
0.1667    0.6667    0.1667  
0.6667   -3.3333    0.6667  
0.1667    0.6667    0.1667
```



```
>> f= fspecial('log')
```

```
f =
```

```
0.0448    0.0468    0.0564    0.0468    0.0448  
0.0468    0.3167    0.7146    0.3167    0.0468  
0.0564    0.7146   -4.9048    0.7146    0.0564  
0.0468    0.3167    0.7146    0.3167    0.0468  
0.0448    0.0468    0.0564    0.0468    0.0448
```



Gaussian filter

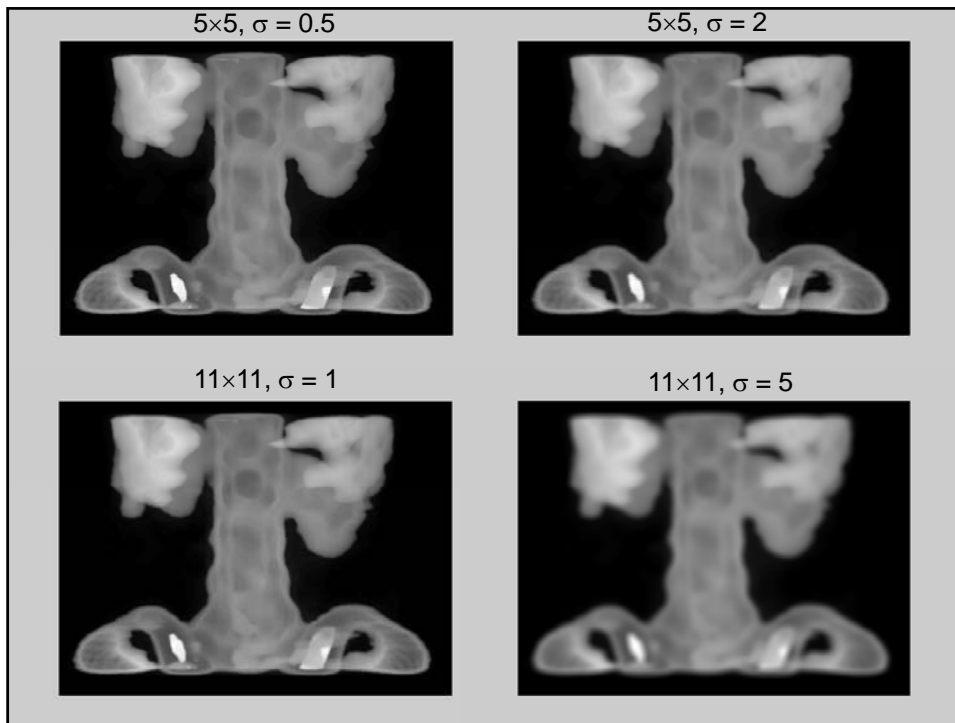
```
- >> f3 = fspecial('gaussian',[5,5]);  
- >> w7= filter2(f3,w);  
- >> imshow(w7/max(max(w7)))
```



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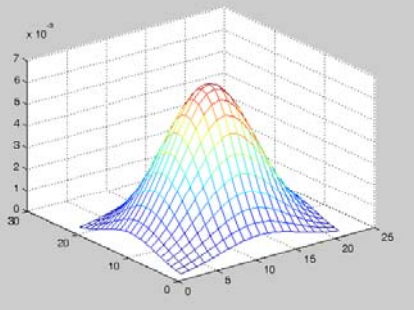
```
- >> f1 = fspecial('gaussian',[5,5],0.5);  
- >> f2 = fspecial('gaussian',[5,5],2);  
- >> f3 = fspecial('gaussian',[11,11],1);  
- >> f4 = fspecial('gaussian',[11,11],5);  
- >> w1= filter2(f1,w);  
- >> w2= filter2(f2,w);  
- >> w3= filter2(f3,w);  
- >> w4= filter2(f4,w);  
- >> figure;imshow(w1/max(max(w1)))  
- >> figure;imshow(w2/max(max(w2)))  
- >> figure;imshow(w3/max(max(w3)))  
- >> figure;imshow(w4/max(max(w4)))
```

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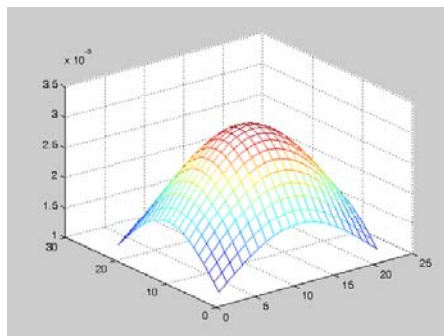


Gaussian filter with different σ

21x21, $\sigma = 5$



21x21, $\sigma = 10$



Fourier Transform by Using Matlab

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Fourier Transform

- “fft” and “ifft” represents the Fourier and inverse Fourier transform

```
>> a= [1 2 3 4 5 6];
```

```
>> fft(a)'
```

```
ans =
```

```
21.0000
```

```
-3.0000 - 5.1962i
```

```
-3.0000 - 1.7321i
```

```
-3.0000
```

```
-3.0000 + 1.7321i
```

```
-3.0000 + 5.1962i
```

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- The `fft(iff(a))` mean the original number itself:

```
>> b =fft(a);
>> ifft(b)

ans =

    1.0000    2.0000    3.0000    4.0000    5.0000    6.0000
```

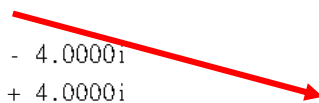
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Shifting property

```
>> x = [2 3 4 5 6 7 8 1];
>> x1 = (-1).^[0:7].*x;
>> fft(x)'

ans =

    4.0000
    1.6569 - 4.0000i
   -4.0000 - 4.0000i
   -9.6569 + 4.0000i
    36.0000
    1.6569 + 4.0000i
    4.0000
   -4.0000 + 4.0000i
    1.6569 - 4.0000i
   -9.6569 - 4.0000i
   -4.0000 + 4.0000i
    1.6569 + 4.0000i
```



```
>> fft(x1)'

ans =

    4.0000
    1.6569 - 4.0000i
   -4.0000 - 4.0000i
   -9.6569 + 4.0000i
    36.0000
    1.6569 + 4.0000i
    4.0000
   -4.0000 + 4.0000i
    1.6569 - 4.0000i
   -9.6569 - 4.0000i
   -4.0000 + 4.0000i
    1.6569 + 4.0000i
```

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2-D Fourier Transform

- `fft2.m` : 2-D Fourier transform
- `ifft2.m`: 2-D inverse Fourier transform
- `fftshift.m`: automatically shift

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Create an useful subroutine for fft plot:

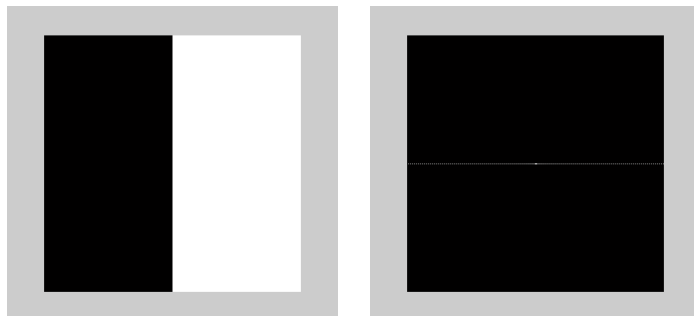
```
function[] = fftshow(f,type)

    if nargin<2,
        type = 'log';
    end;

    if (type == 'log'),
        f1 = log(1+abs(f));
        fm = max(f1(:));
        imshow(im2uint8(f1/fm));
    elseif (type == 'abs'),
        fa = abs(f);
        fm = max(fa(:));
        imshow(fa/fm);
    else,
        error('TYPE must be abs or log.');
```

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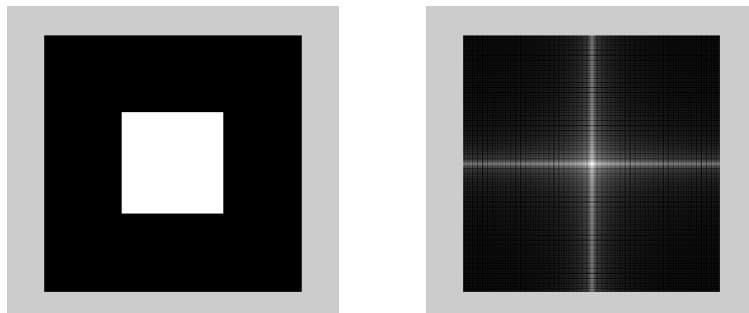
```
- >> a = [zeros(256,128), ones(256,128)];  
- >> af = fftshift(fft2(a));  
- >> figure;imshow(a)  
- >> figure;fftshow(af)
```



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FFT for a rectangular function

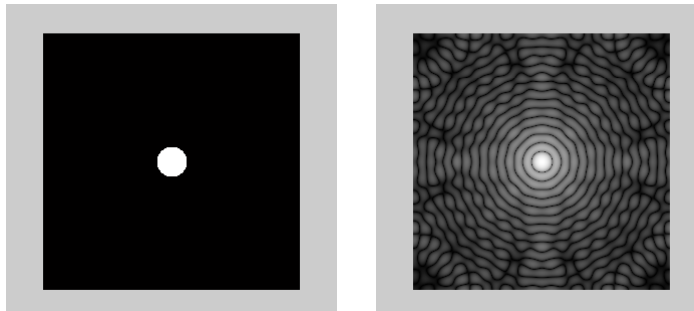
```
- >> a = zeros(256,256);  
- >> a(78:178,78:178) = 1;  
- >> af = fftshift(fft2(a));  
- >> figure;imshow(a)  
- >> figure;fftshow(af,'log')
```



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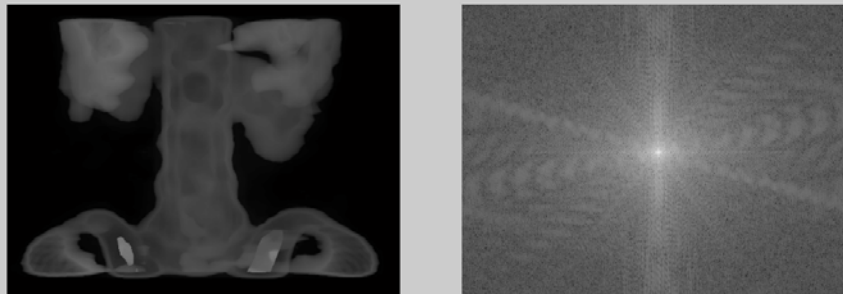
FFT for a circular function

- `>> [x,y]=meshgrid(-128:127,-128:127);`
- `>> z = sqrt(x.^2+y.^2);`
- `>> c = (z<15);`
- `>> cf = fftshift(fft2(c));`
- `>> figure;imshow(c)`
- `>> figure;fftshow(cf,'log')`



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- Original image and its Fourier transform:



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An example for low-pass filter

```
- >> w=imread('cameraman.tif');  
- >> f = fftshift(fft2(w));  
- >> cf = c.*f;  
- >> cfi = ifft2(cf);  
- >> figure;imshow(cfi/max(max(cfi)))  
- >> figure;fftshow(cf,'log')
```

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Original image



fftshow(cf, 'log')

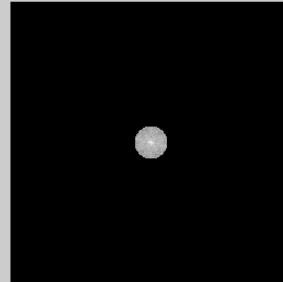


Image after filtering
→ Ringing effect can be found !

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An example for high-pass filter

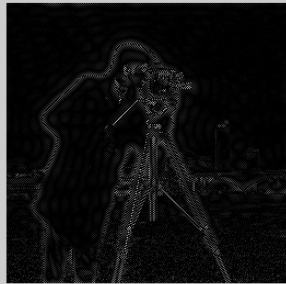
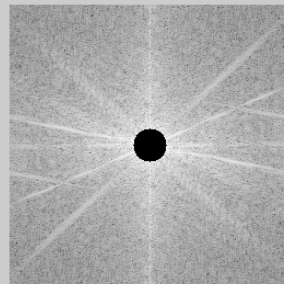
- `>> [x,y]=meshgrid(-128:127,-128:127);`
- `>> z = sqrt(x.^2+y.^2);`
- `>> c = (z>15);`
- `>> f = fftshift(fft2(w));`
- `>> cf = c.*f;`
- `>> cfi = ifft2(cf);`
- `>> figure;fftshow(cf,'log')`
- `>> figure;imshow(cfi/max(max(cfi)))`

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Original image



fftshow(cf, 'log')



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Exercise

- Create a 2-D Gaussian function to erase the ringing effect caused by a rigid low-pass filter in the “caremaman.tif” image.

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Reconstructing an Image from Projection Data (Parallel Beam)

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Create phantom

- A shape-and-logan phantom (left in your homework)



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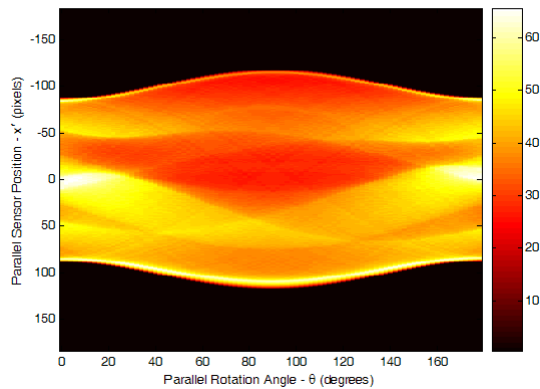
Radon transform

```
- >> theta1 = 0:10:170;  
- >> [R1, xp] = radon(P, theta1);  
- >> theta2 = 0:5:175;  
- >> [R2, xp] = radon(P, theta2);  
- >> theta3 = 0:2:178;  
- >> [R3, xp] = radon(P, theta3);
```

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Plot the radon transform

- `Figure; imagesc(theta3,xp,R3);`
- `colormap(hot)`
- `colorbar`
- `xlabel('Parallel Rotation Angle - \theta (degrees)');`
- `ylabel('Parallel Sensor Position - x\prime (pixels)');`



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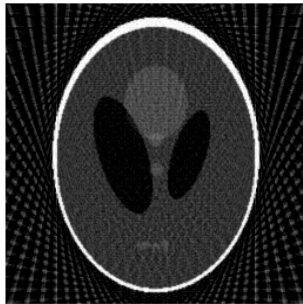
Image reconstruction using “iradon.m”

- `>> dtheta1 = theta1(2) - theta1(1);`
- `>> I1 = iradon(R1,dtheta1,256);`
- `>> figure; imshow(I1);`



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```
- >> output_size = 256;  
- >> dtheta2 = theta2(2) - theta2(1);  
- >> I2 = iradon(R2,dtheta2,output_size);  
- >> figure, imshow(I2);
```



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```
- >> dtheta3 = theta3(2) - theta3(1);  
- >> I3 = iradon(R3,dtheta3,output_size);  
- >> figure, imshow(I3);
```



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How to create matrix variable?

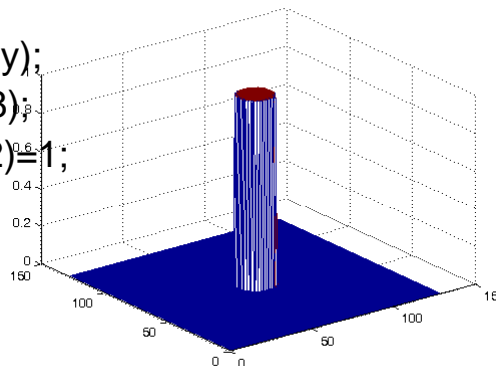
- Meshgrid.m `>> [X,Y] = meshgrid(-2:.2:2, -2:.2:2);`
- Zeros.m `>> Z = X .* exp(-X.^2 - Y.^2);`
- Ones.m
- Special functions `>> mesh(Z)`
`>> zeros(5)`
 - Peaks.m
- Others: `ans =`
 - See “demo”...

```
0 0 0 0 0
```

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How to create circle?

- Example:
`>> x = -64:63;`
`>> y = -64:63;`
`>> [X,Y]=meshgrid(x,y);`
`>> Z = zeros(128,128);`
`>> Z(X.^2+Y.^2<10^2)=1;`
`>> mesh(Z)`



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